

Operation Of Project X Linac As A Driver For Muon Collider

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Fermilab TD and AD

Motivation and Outline

- Baseline Project X design is well established
 - ▶ CW operation with 1 mA average current at 3 GeV; pulsed 3-8 GeV
- Project X is considered as a beam source for a future Neutrino Factory and/or Muon Collider
 - ▶ 15 Hz pulses of 6.7 ms with 5 mA average and 10 mA peak current
 - 3-4 MW at 8 GeV
- In this study we address issues associated with operation of Project X linac (specifically, HE 650 MHz section) as a driver for Muon Collider
 - ▶ Coupling optimization
 - ▶ Incoherent losses
 - ▶ Resonance excitation of HOMs
 - cryogenic losses
 - emittance increase
 - ▶ Collective effects

Coupler Optimization

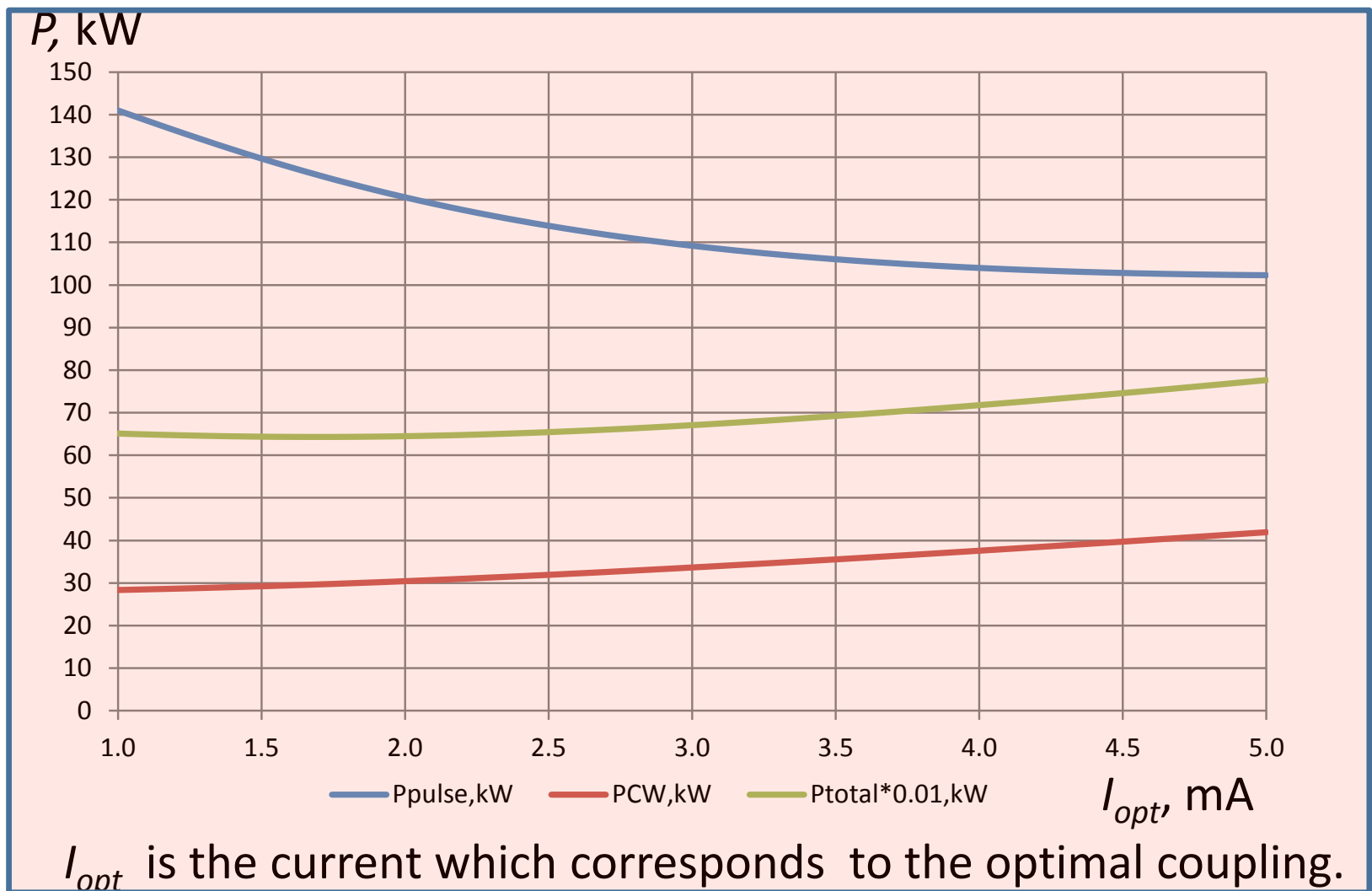
$f = 650 \text{ MHz}$
 $\delta f = 18 \text{ Hz}$ - microphonics
 $(R/Q) = 640 \text{ Ohm}$
 $I_{CW} = 1 \text{ mA}$ - DC current
 $I_{pulse} = 5 \text{ mA}$ - pulse current
 $\varphi = -10^\circ$ - synch. phase
 $V = 17.5 \text{ MV}$ - gain/cavity
 $\tau = 6.7 \text{ ms}$ - pulse width
 $f_{rep} = 15 \text{ Hz}$ - rep. rate
 $N = 160$ - number of cavities
 16% overhead

$$Q_{load}(1\text{mA}) = 1.5e7$$

$$Q_{load}(2\text{mA}) = 1.1e7$$

$$P_{CW}(1\text{mA}) = 28 \text{ kW}$$

$$P_{CW}(2\text{mA}) = 30 \text{ kW}$$



$$P_{total} = N(P_{CW}(1 - f_{rep} \tau) + P_{pulse} f_{rep} \tau)$$

- Total power is minimal if coupler is optimized for 2 mA. RF source should provide power of 120 kW in 10% duty cycle
- It is possible to use coupling for 2 mA; it will take 7% more power for the period before MC
- Better to use coupling tuned for 1 mA and adjust coupling when MC is built

Incoherent Losses

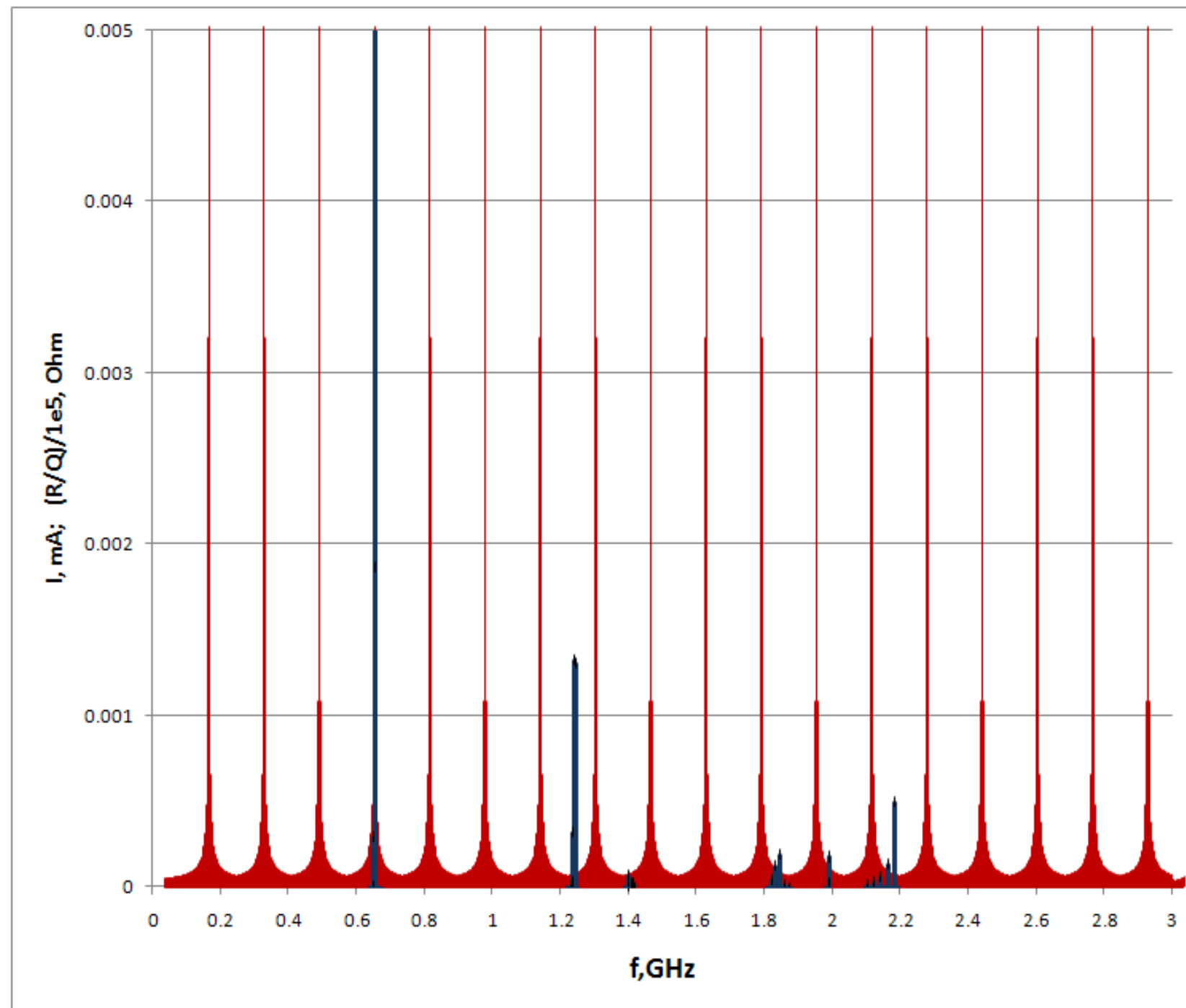
- MC pulses (5mA average current, 10% DF, 10mA peak current)
 - ▶ Average current increases by factor of 1.4
 - ▶ Incoherent losses increase 1.9 times

	ProjectX	SNS	ILC
I_{av}, mA	$I(PX)/1.4(PX+MC)$	1	4.80E-02
Q_b, pC	$25.6(PX)/51.2(MC)$	58	3200
$k_{loss}, \text{V/pC}$	2	1.1	13.4
$P_{av}, \text{mW/cavity}$	$51(PX)/97(PX+MC)$	64	2065

- Incoherent losses are small

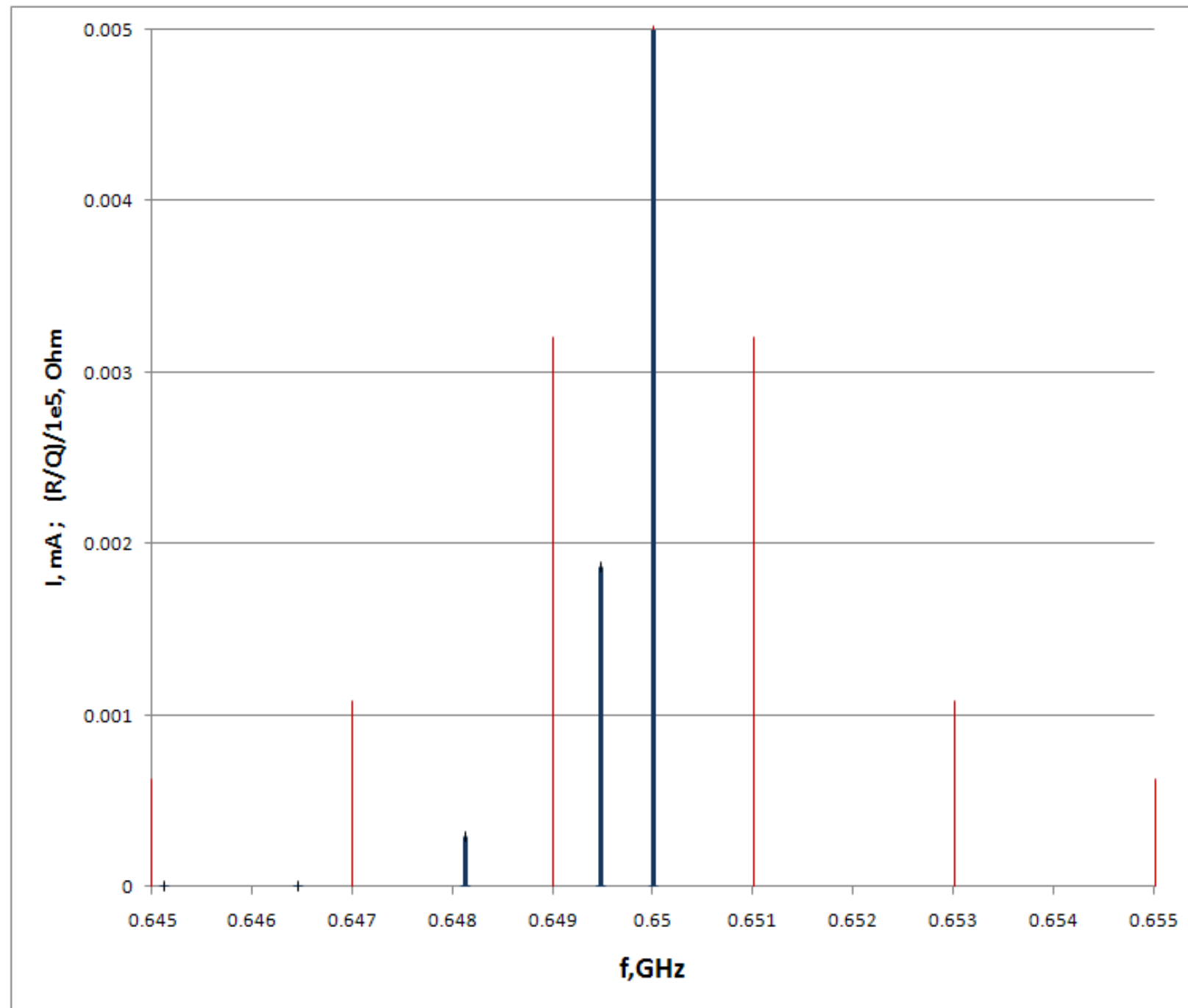
Beam and HOMs spectra

- Idealized beam spectrum: 1 μ s period, 50% DF
- HE 650 MHz cavity impedance



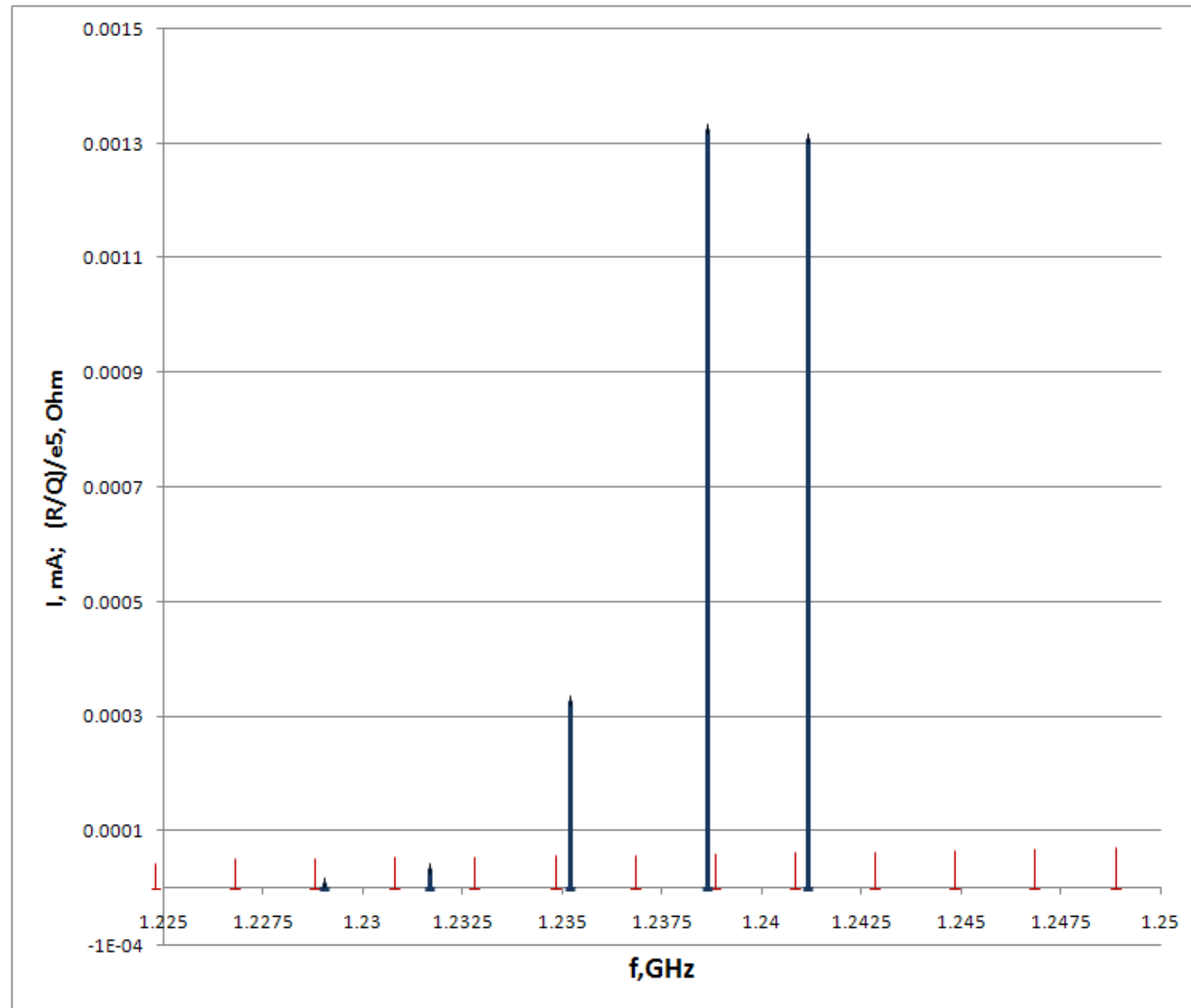
- Strong cavity resonances fall between main beam spectrum lines; HOM frequency spread \sim 1 MHz

1st Passband (Operating)



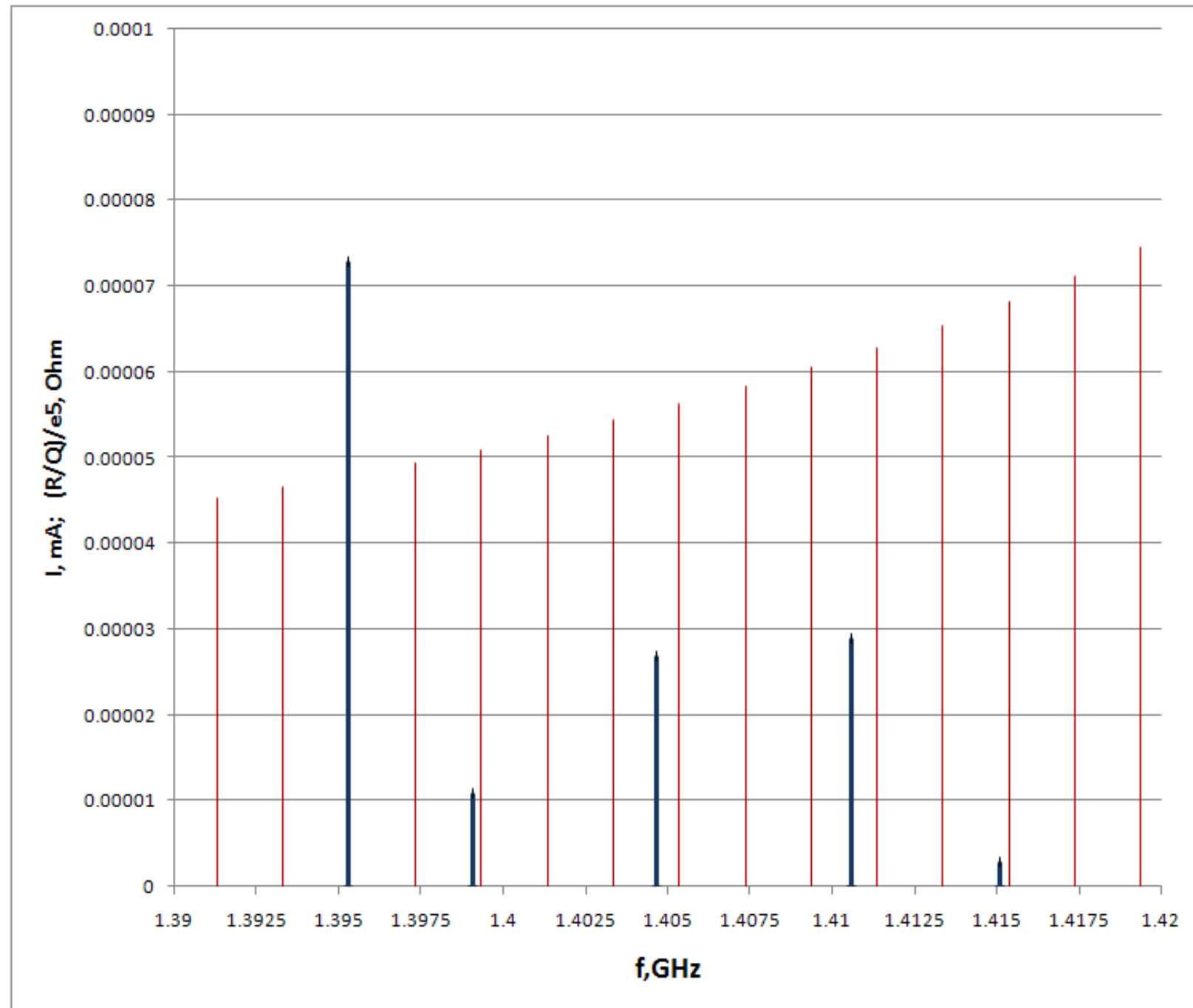
- 4th mode falls between operating frequency and a side band frequency. This mode is strongly coupled to the main coupler

2nd Passband



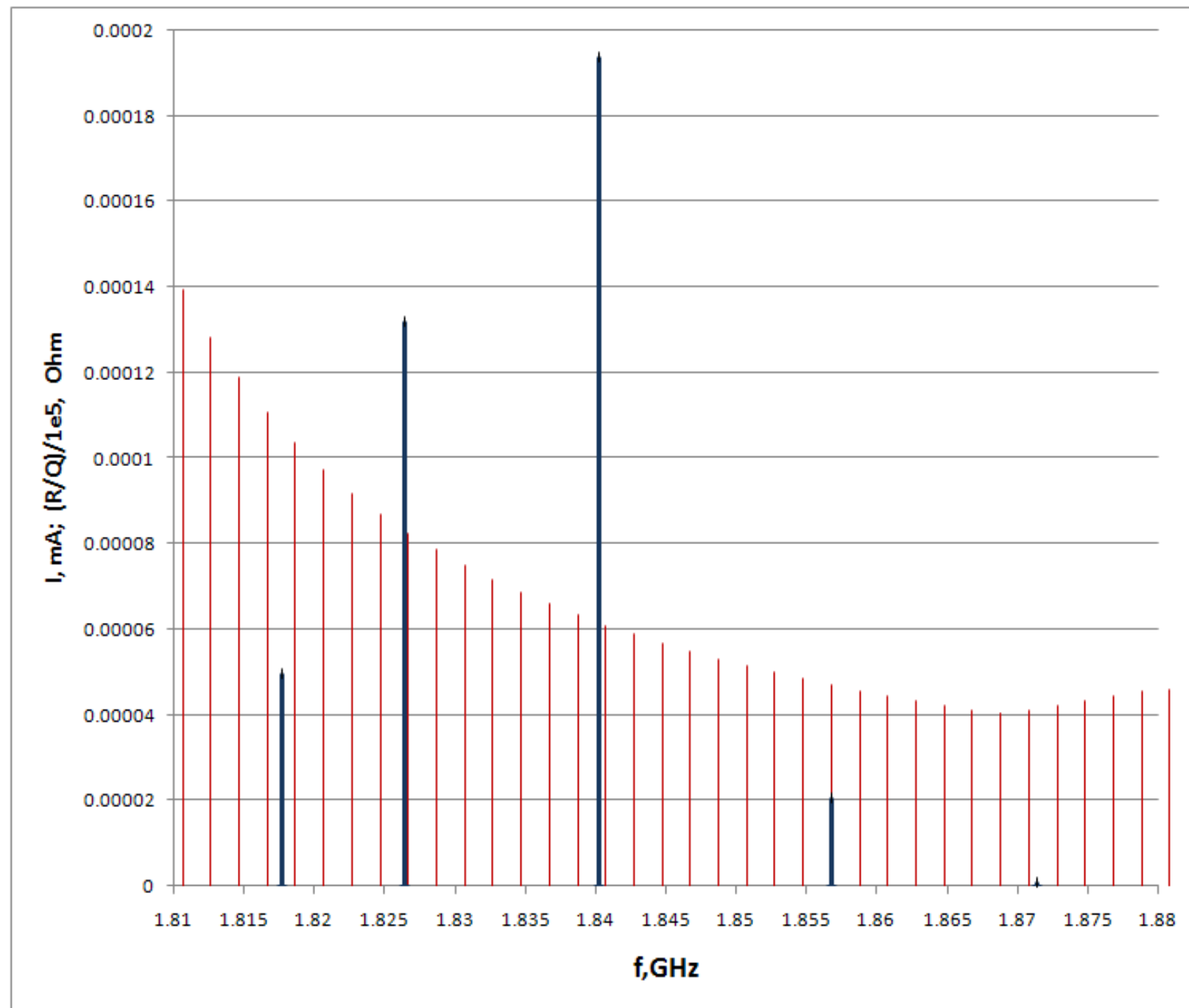
- Mode frequencies are located far off the lines of beam spectrum; nearest line of beam spectrum has current $< 10 \mu\text{A}$

3d Passband



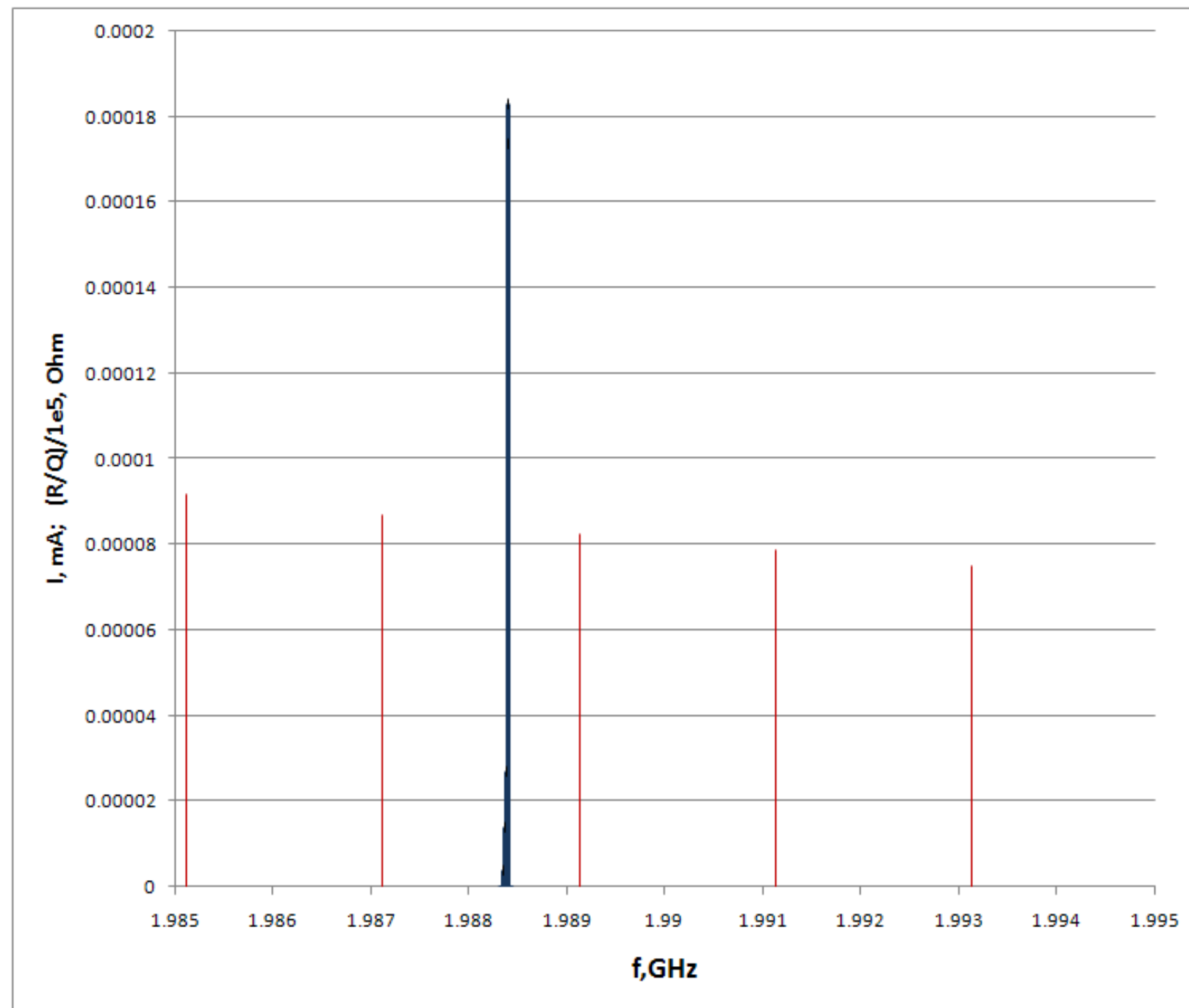
- Mode frequencies are located far off the lines of beam spectrum; nearest line of beam spectrum has current $< 10 \mu\text{A}$

4th Passband



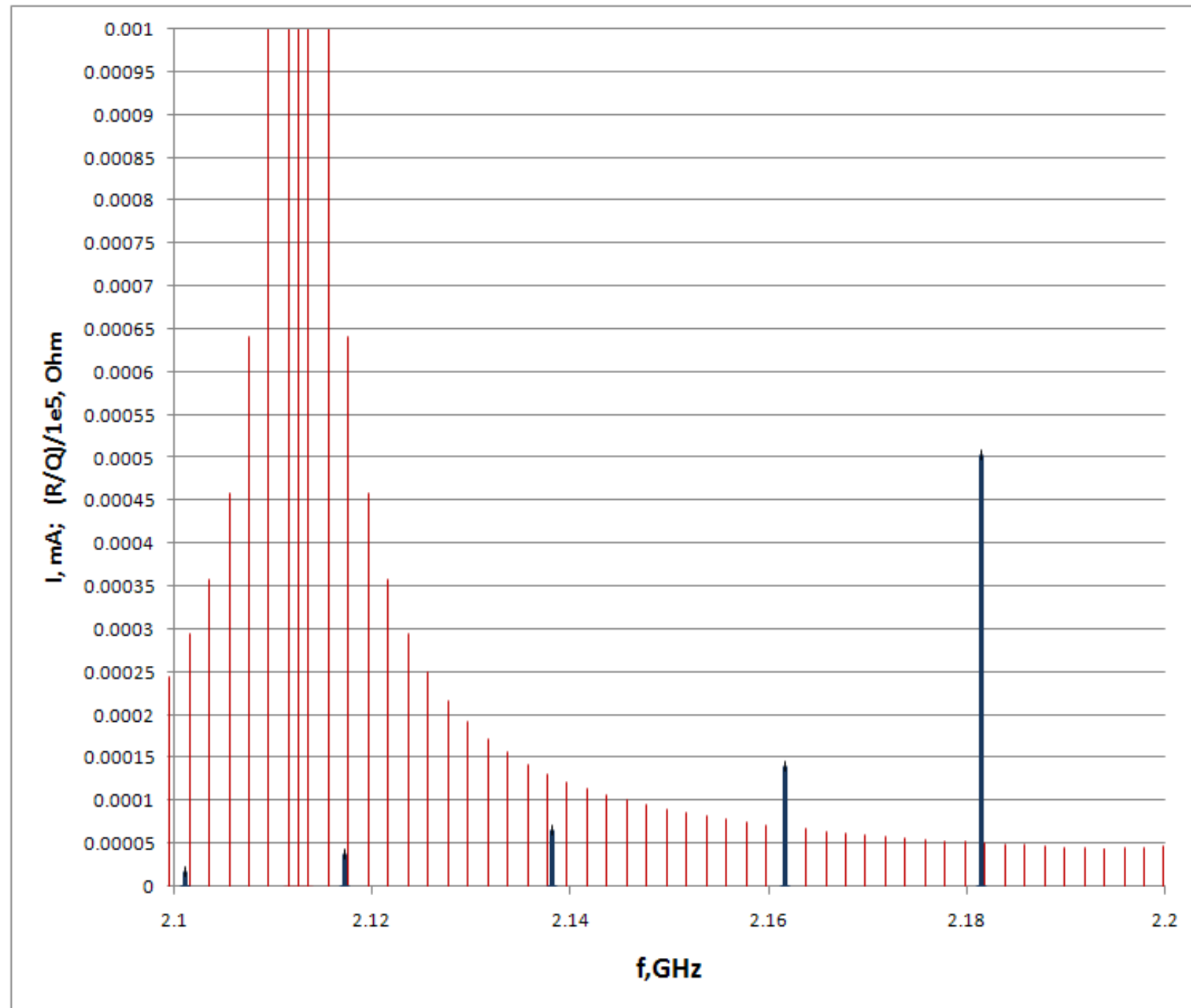
- Mode frequencies are located far off the lines of beam spectrum; nearest line of beam spectrum has current $< 10 \mu\text{A}$

5th Passband



- Mode frequencies are located far off the lines of beam spectrum; nearest line of beam spectrum has current $< 10 \mu\text{A}$

6th Passband



- Mode frequencies are located far off the lines of beam spectrum; nearest line of beam spectrum has current $< 10 \mu\text{A}$

Resonance Excitation Of Monopole HOMs

- Longitudinal beam emittance ($\epsilon_z = 1.6 \text{ keV*ns}$) should not increase due to interaction with monopole modes
- If U_{HOM} is average gain caused by HOM, σ_t is bunch length, then $U_{HOM} \sigma_t \ll \epsilon_z$
- For high- Q resonances ($\delta f/f \gg 1/Q$, \tilde{I} is beam spectrum line amplitude):

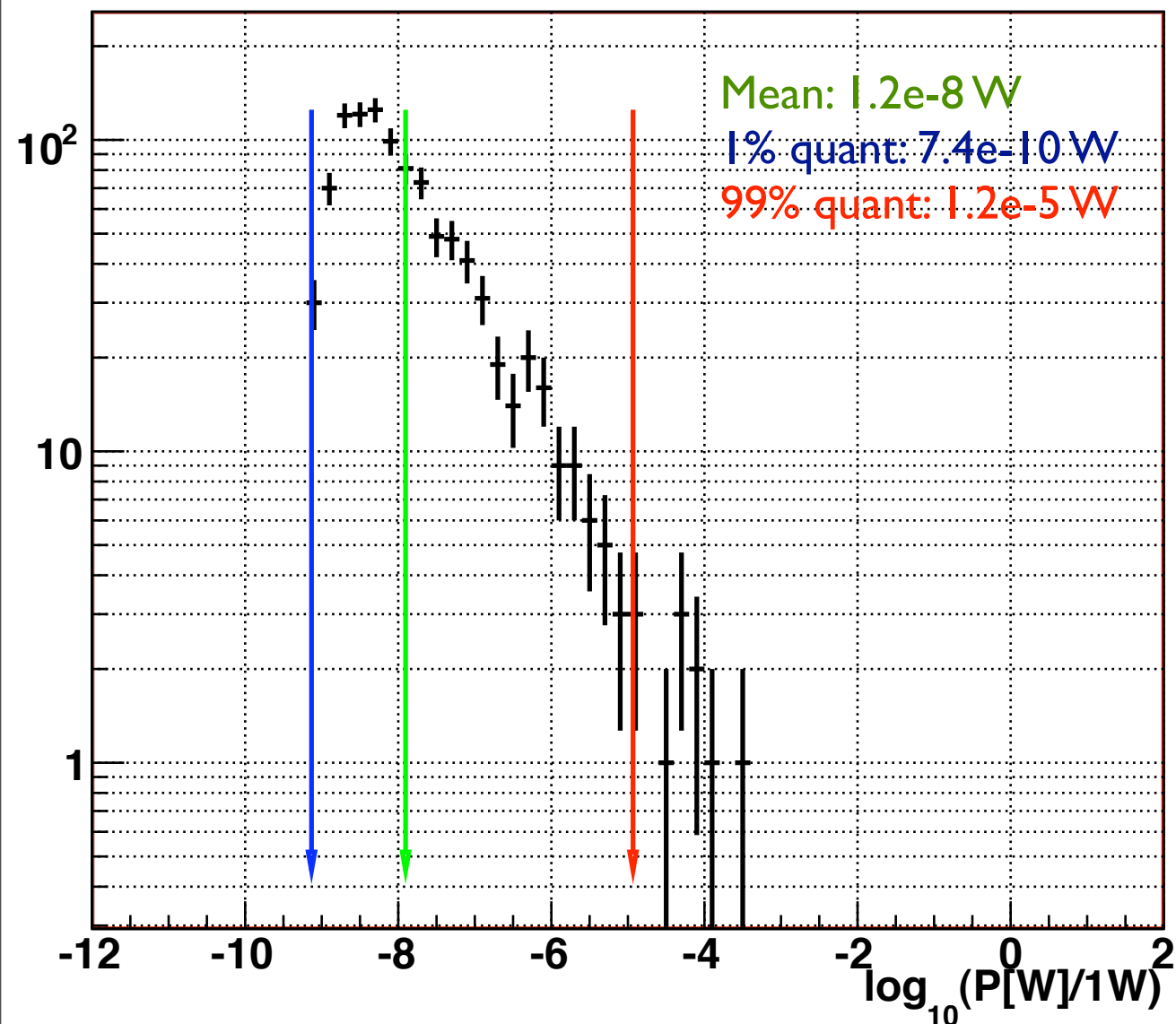
$$U_{HOM} \approx \frac{\tilde{I}(R/Q)}{4\sqrt{2}\delta f/f}, \delta f \gg f \frac{\tilde{I}(R/Q)\sigma_t}{4\sqrt{2}\epsilon_z}$$

- For example, for beam line with frequency $f = 1395.2 \text{ MHz}$, $\tilde{I} = 5 \text{ uA}$, $(R/Q) = 7 \text{ Ohm}$, and $\sigma_t = 7.7 \text{ ps}$ (1.8 deg), $\delta f \gg 0.04 \text{ Hz}$
- Other example: beam line with frequency $f = 1241 \text{ MHz}$, $\tilde{I} = 5 \text{ uA}$, $(R/Q) = 130 \text{ Ohm}$, $\delta f \gg 0.7 \text{ Hz}$
- Resonance excitation of monopole HOMs does not seem to be a problem

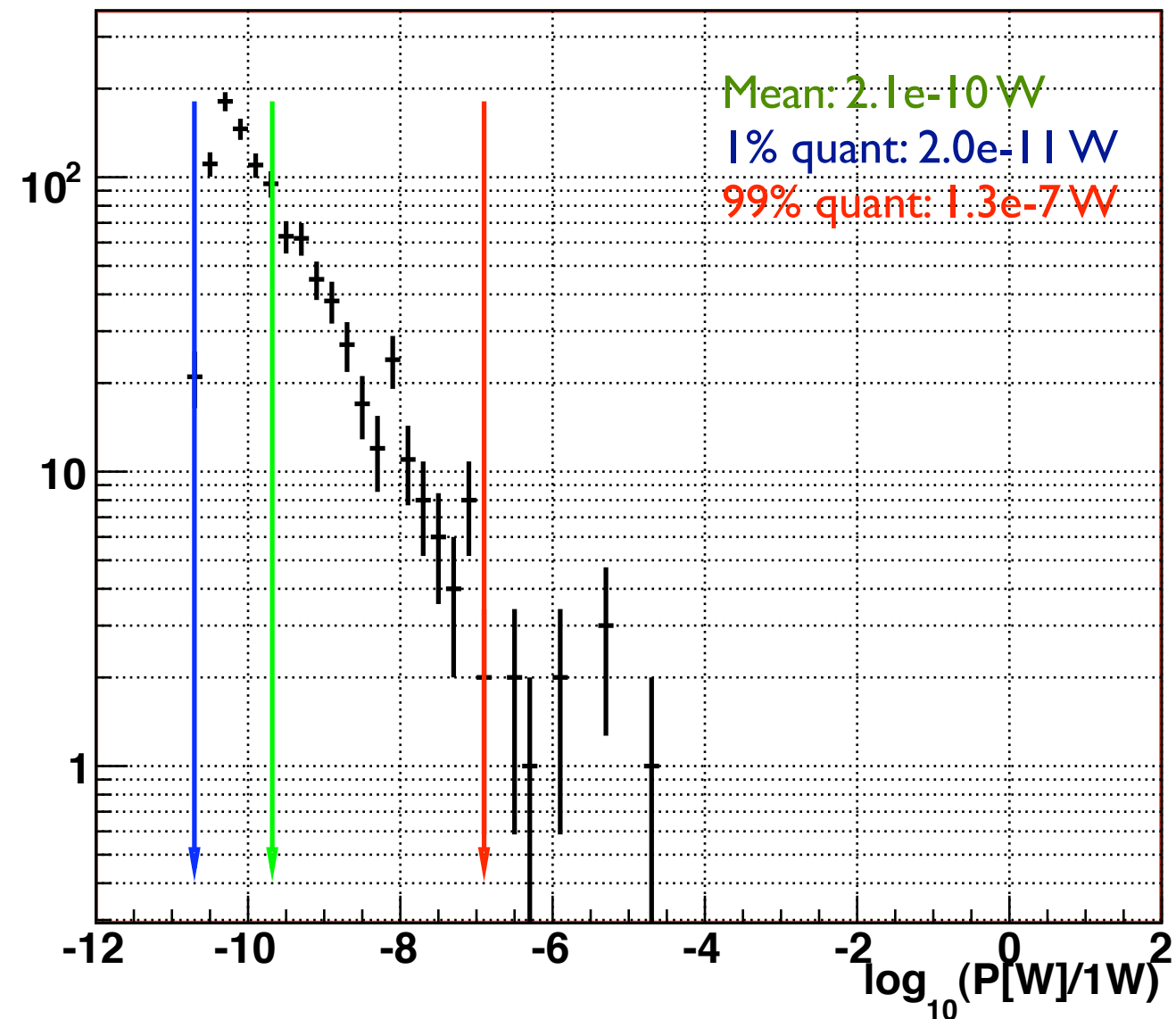
Resonance Excitation of Monopole HOMs

- Power loss in cavity walls, non-propagating monopole HOMs ($f < 2.3\text{GHz}$)
 - Distribution of losses is due to spread of HOM frequencies (1 MHz R.M.S.)

Project X beam structure



Muon Collider beam structure



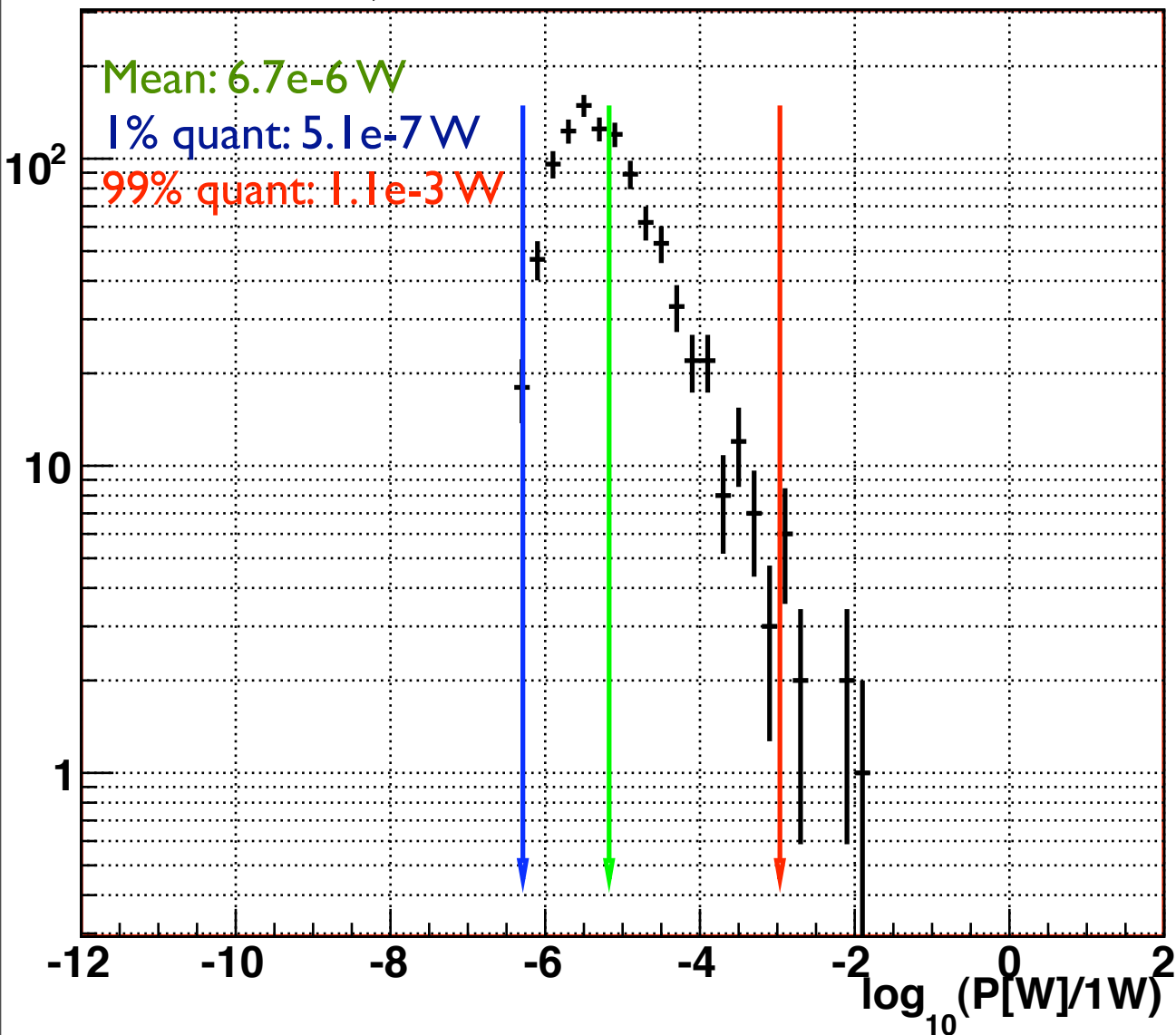
Resonance Excitation of Monopole HOMs

- Power loss in cavity walls, propagating monopole HOMs
- Beam pipe ($r=5$ cm) cut-off frequency: $f = 2.3\text{GHz}$
 - ▶ Most of HOMs w/ frequency above cut-off escape from cavities
 - ▶ Some of them may become trapped in cavities
 - reflection and interference with HOMs from adjacent cavities
- Use *VERY* conservative estimation of power loss upper limit:
 - ▶ Simulate cavity with beam pipe of length L ($= 10\text{-}40$ cm) on both ends
 - ▶ Consider that *all* HOMs w/ frequency above cut-off are trapped in cavities
 - ▶ Use maximum values of (R/Q) w.r.t. beam pipe length L and particle velocity
- Justify this approach by results
 - ▶ If this method shows that losses are still small, no need to worry about them

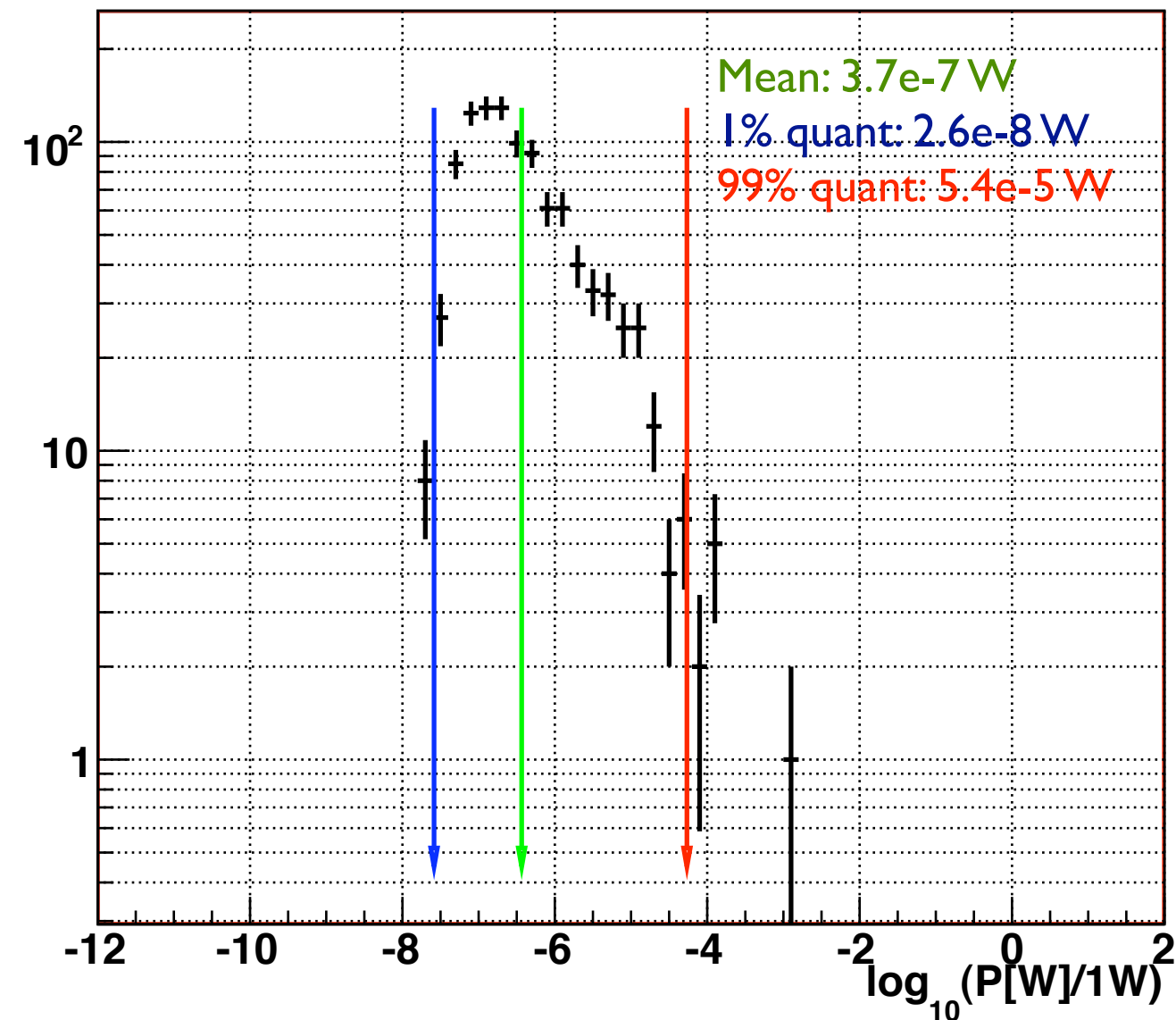
Resonance Excitation of Monopole HOMs

- Power loss in cavity walls, propagating monopole HOMs ($f > 2.3\text{GHz}$)

Project X beam structure



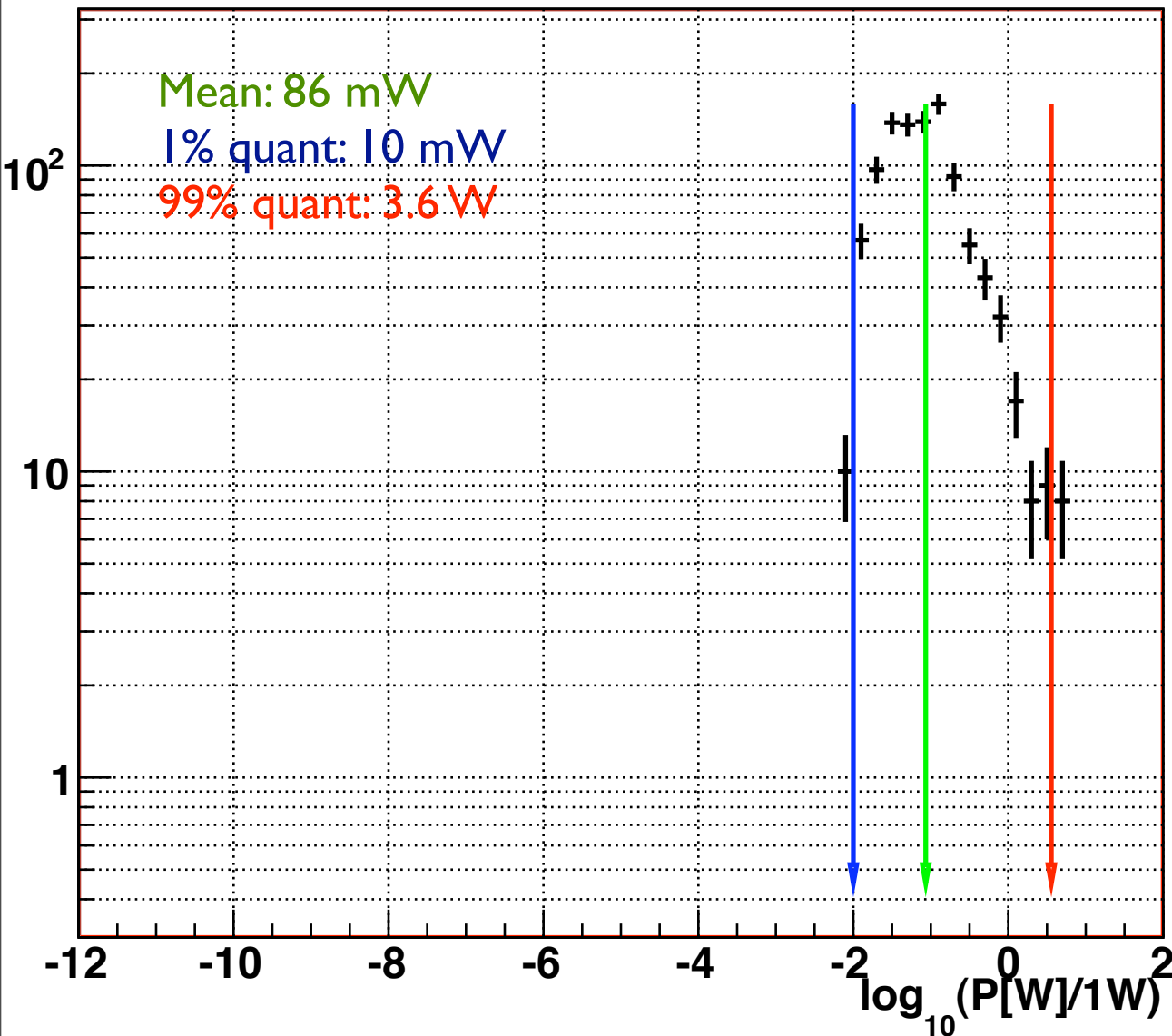
Muon Collider beam structure



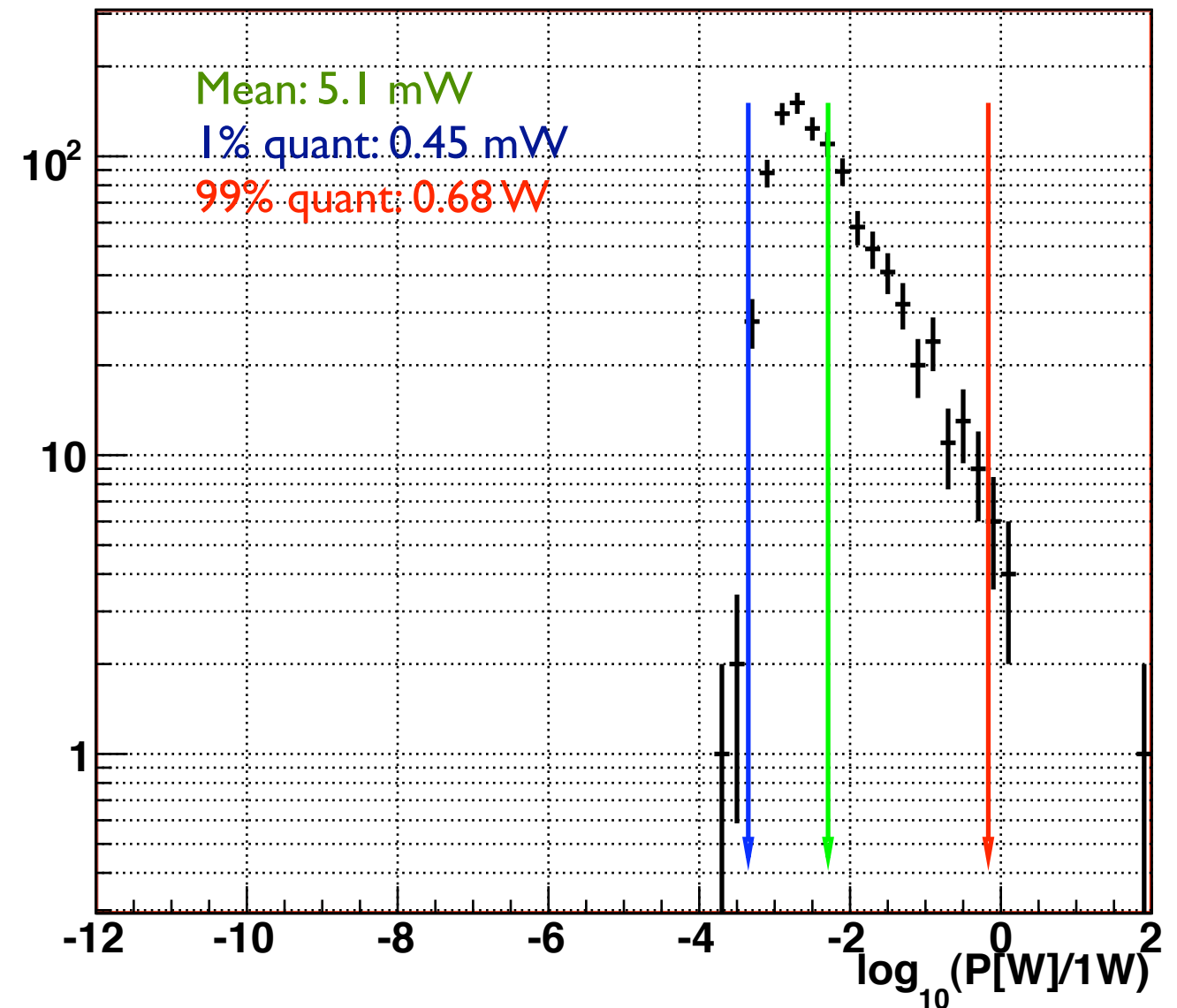
Resonance Excitation of Monopole HOMs

- Power loss in bellows, propagating monopole HOMs ($f > 2.3\text{GHz}$)

Project X beam structure



Muon Collider beam structure

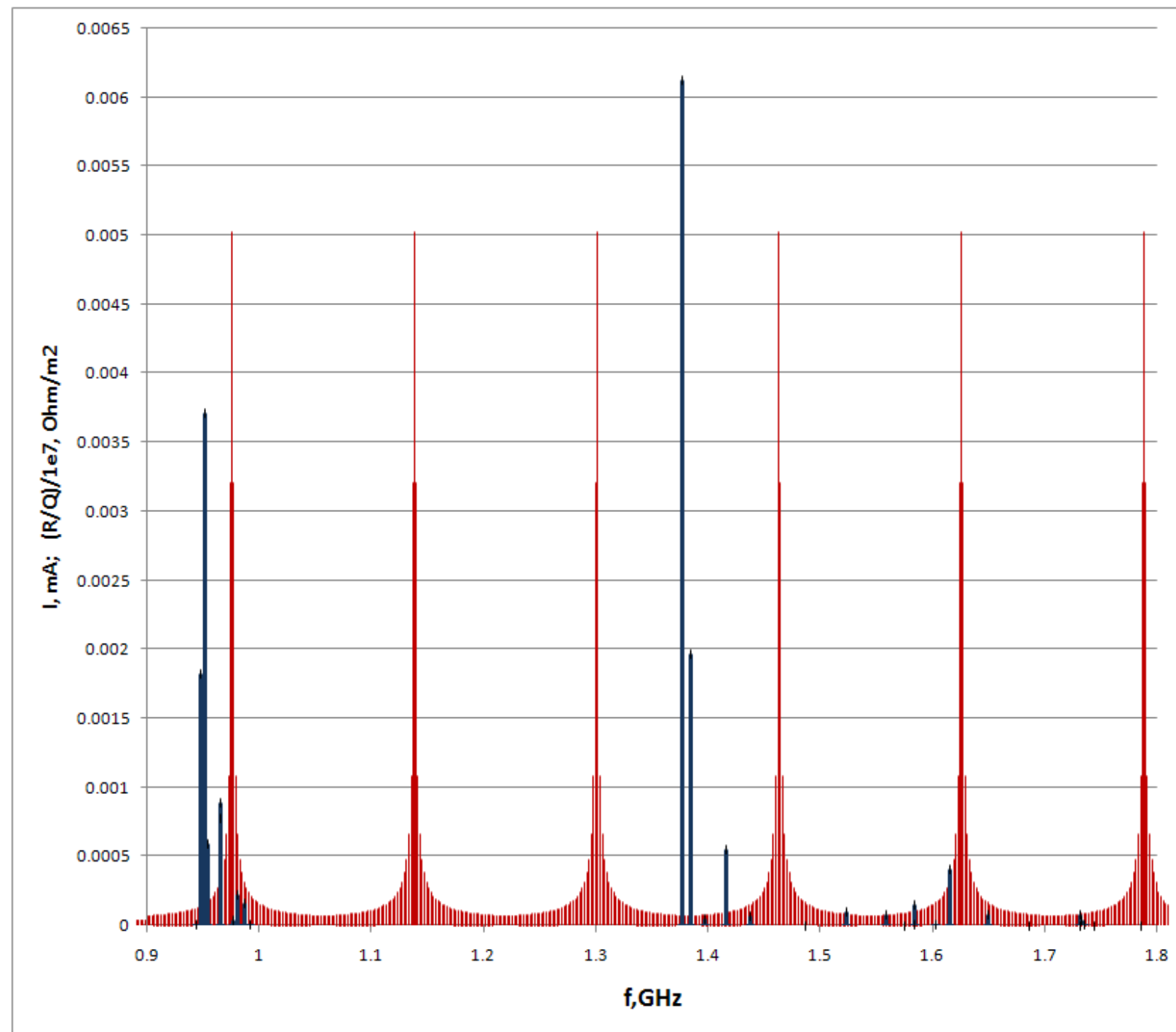


Resonance Excitation of Monopole HOMs: Summary

Power Loss, W	Project X beam structure			Muon Collider beam structure		
	Cav. non-prop. HOMs	Cav. prop. HOMs	Bellows	Cav. non-prop. HOMs	Cav. prop. HOMs	Bellows
Mean	1.20E-08	6.70E-06	0.086	2.10E-10	3.70E-07	5.10E-03
1% quantile	7.40E-10	5.10E-07	0.010	2.00E-11	2.60E-08	4.50E-04
99% quantile	1.20E-05	1.10E-03	3.6	1.30E-07	5.40E-05	0.68

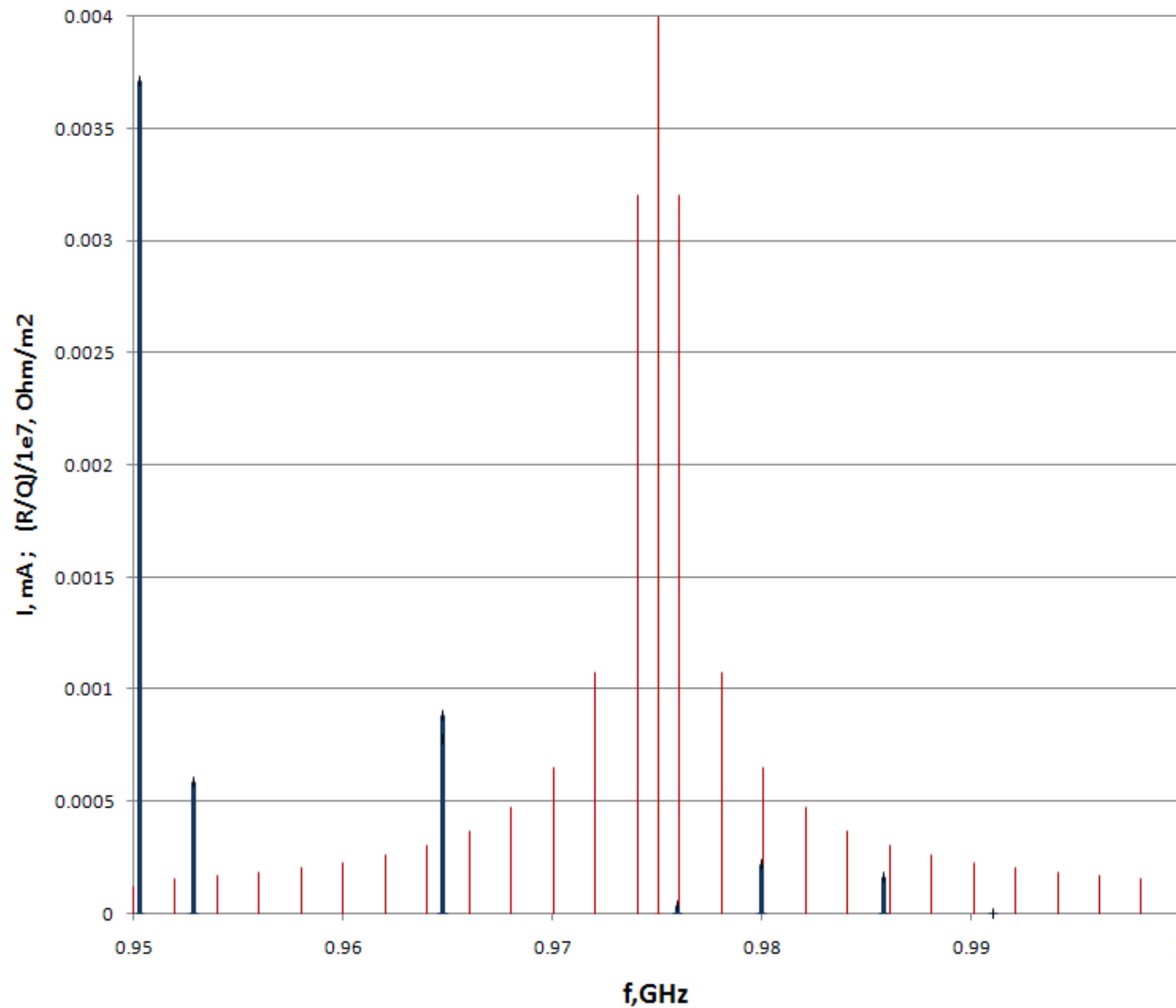
- Muon Collider beam power loss due to resonance excitation of monopole HOMs in HE 650 MHz cavities is a small fraction compared to the power loss of the standard Project X beam structure

Beam Spectrum And Dipole HOMs



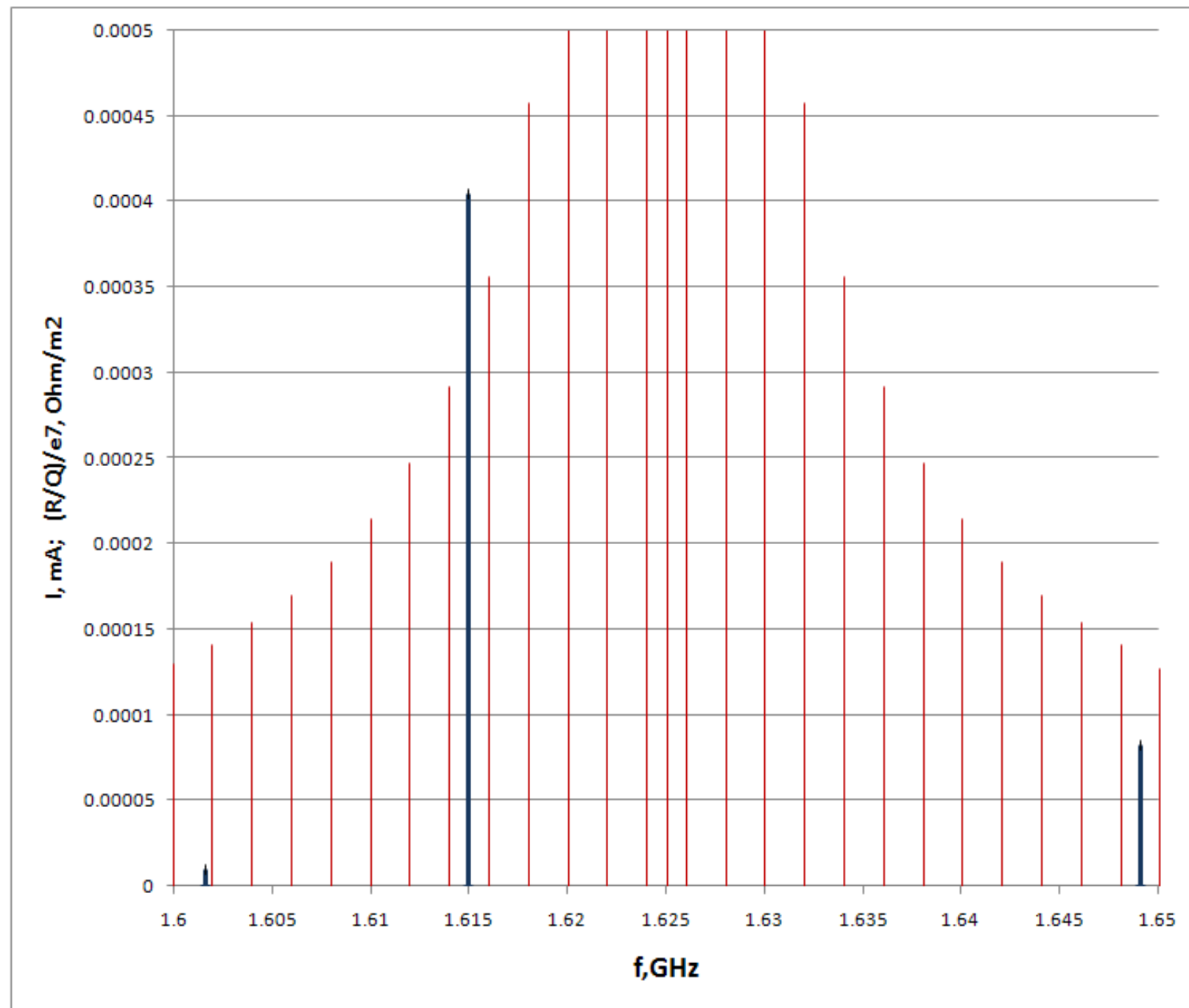
- All strong resonances are far from the main beam spectrum lines

Beam Spectrum And Dipole HOMs At 975 MHz



- Mode with the frequency of 950 MHz has impedance of 37 kOhm/m², while the nearest beam spectrum line is 0.2 mA

Beam Spectrum And Dipole HOMs At 1625 MHz



- Mode with the frequency of 1615 MHz has impedance of 4 kOhm/m², while the nearest beam spectrum line is 0.35 mA

Resonance Excitation Of Dipole HOMs

- Dipole modes should not increase the beam transverse emittance ($\varepsilon=2.5\text{e-}7/\beta\gamma$ m)
- Transverse kick caused by the HOMs ($k=2\pi/\lambda$)

$$U_{\text{kick}} \approx \frac{f}{4\delta f} \left(\frac{x_0}{k} \right) \tilde{I}(R/Q)_1, \delta f/f \gg 1/Q$$

- Emittance increase (β_f is beta-function at the cavity)

$$\delta\varepsilon \approx \Delta x' \sigma_x = \frac{U_{\text{kick}}}{\sqrt{2}p_{\parallel}c} \sqrt{\varepsilon\beta_f}$$

- Condition of small increase of emittance ($\delta\varepsilon \ll \varepsilon$, U_0 is proton rest energy)

$$\delta f \gg \frac{cx_0 \tilde{I}(R/Q)_1}{8\sqrt{2}\pi\beta\gamma U_0 \sqrt{\varepsilon/\beta_f}}$$

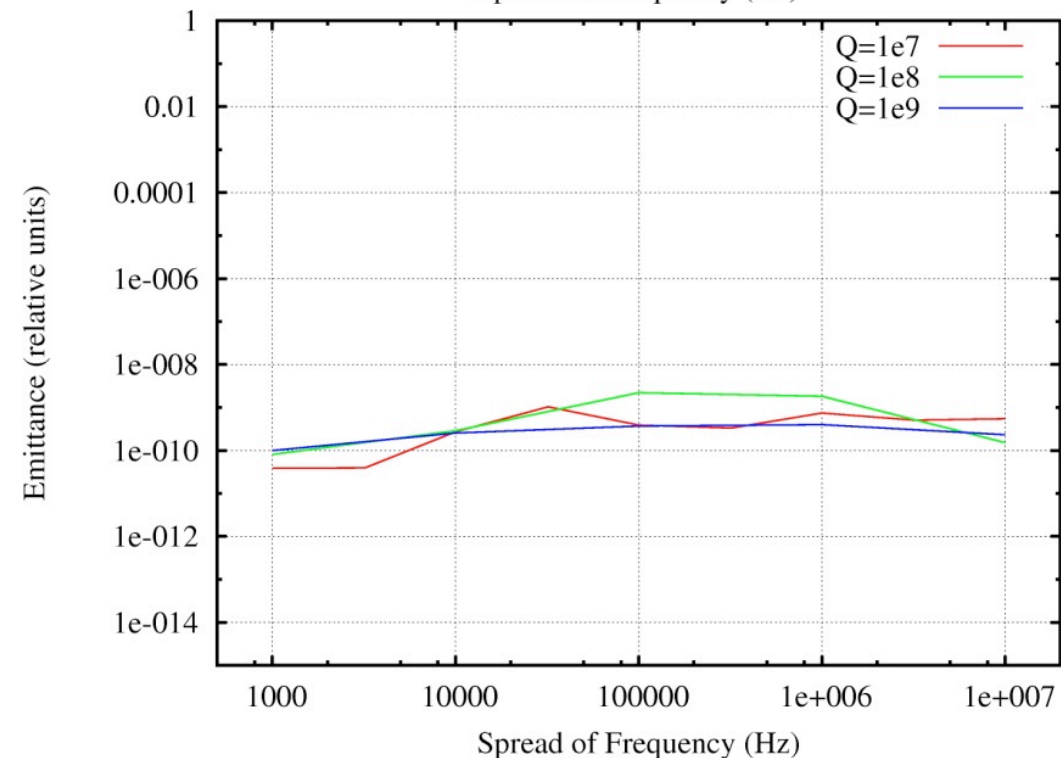
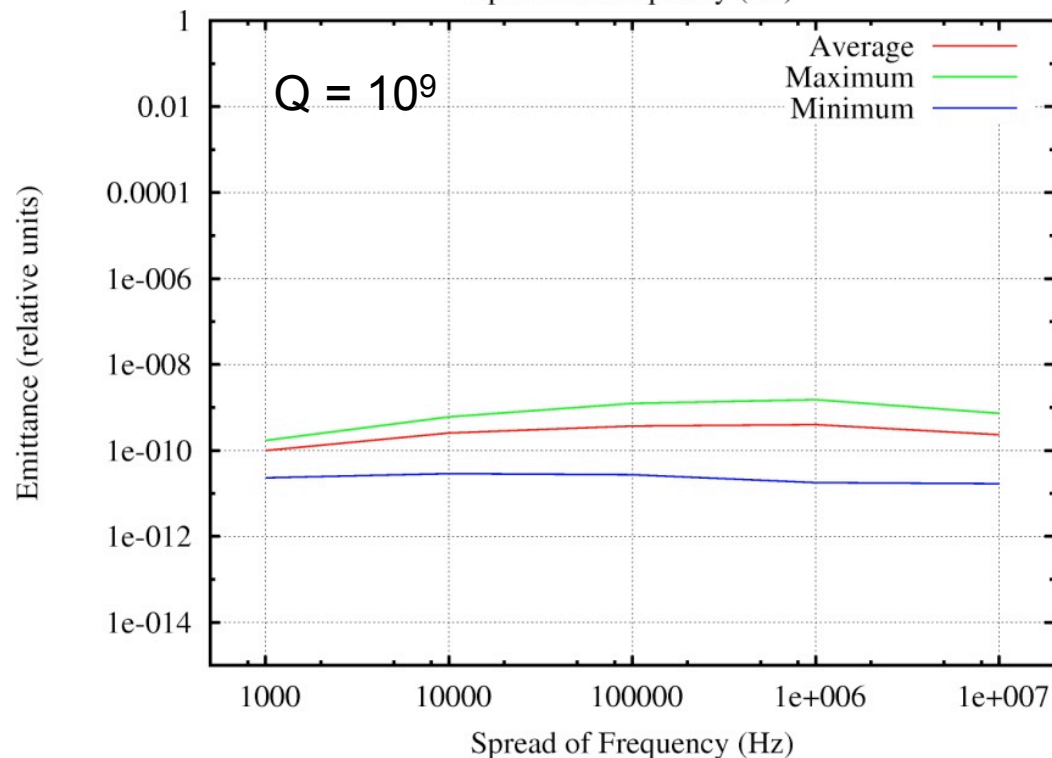
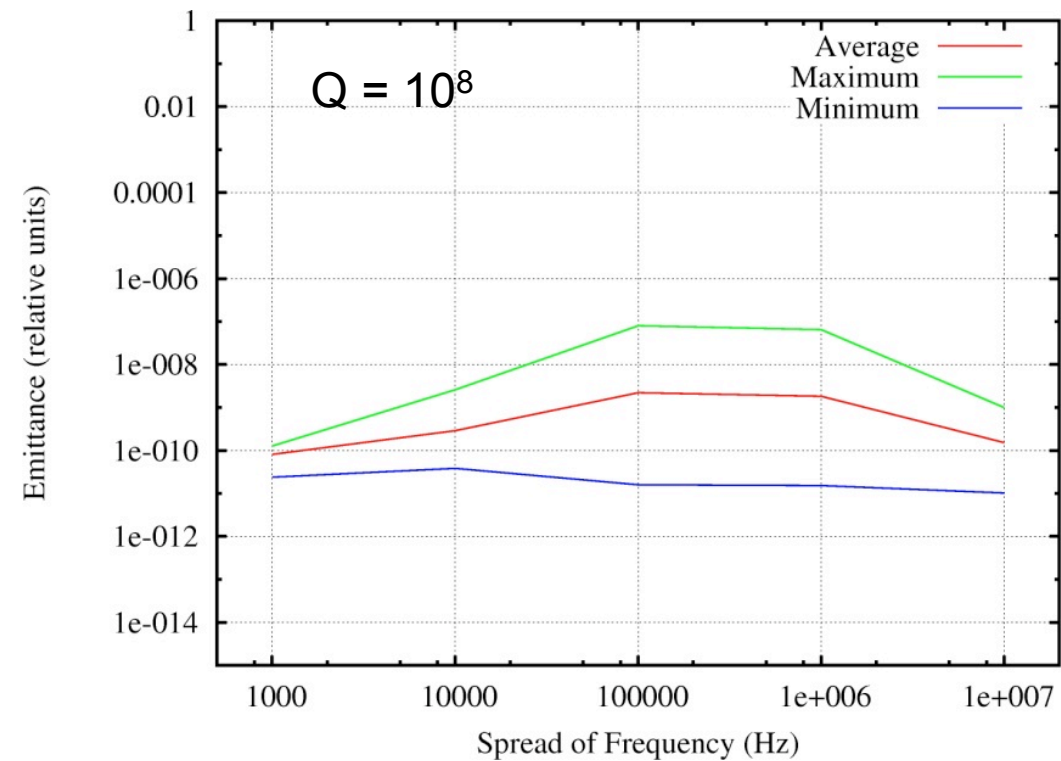
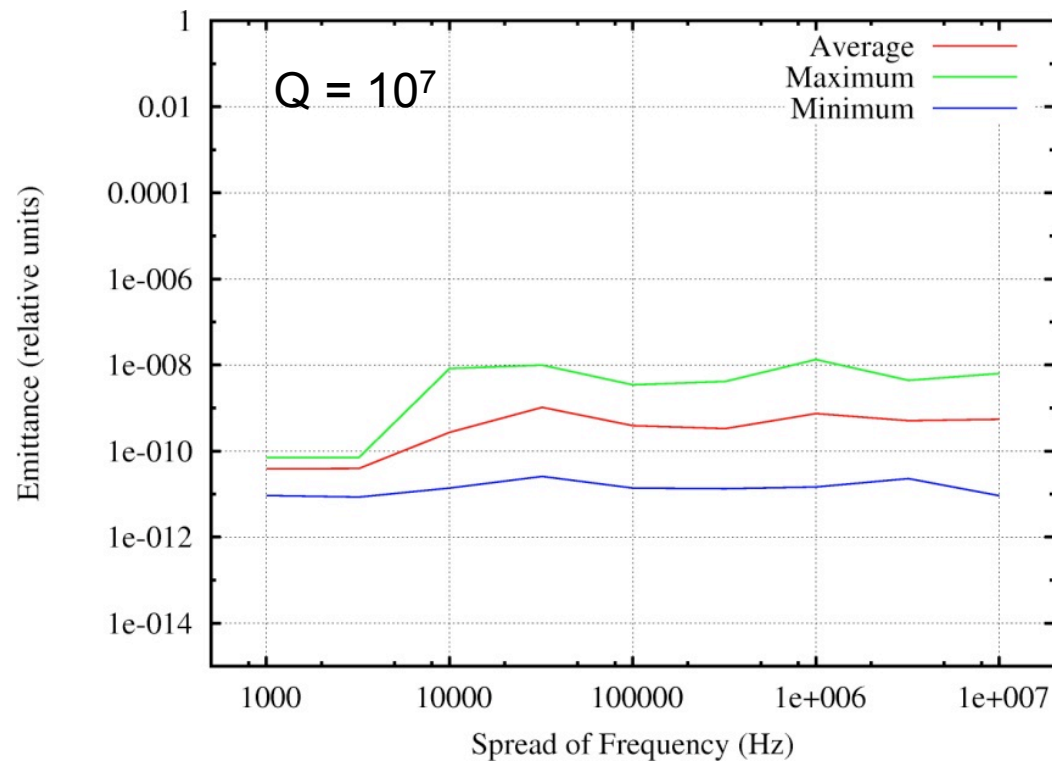
- For example, for mode $f=950$ MHz, $(R/Q)_1=37$ kOhm/m², proton energy 500 MeV, $\beta_f=15$ m, beam spectrum line current 2 mA, $x_0=1$ mm one has: $\delta f \gg 5$ Hz
- Not a problem!

Collective Effects

- Beam break-up (BBU), transverse
- “Klystron-type”, longitudinal
- Why collective effects may not be an issue
 - ▶ No feedback as in CEBAF
 - ▶ Different cavity types with different frequencies and different HOM spectrum
 - ▶ HOMs frequency spread in each cavity type due to manufacturing tolerances
 - ▶ HOMs (R/Q) dependence on velocity
 - ▶ Relatively small beam current
- Simulation shows that relative increase in both transverse and longitudinal emittances is very small and we have safety margin of few orders of magnitude

Collective Effects: Transverse Emittance

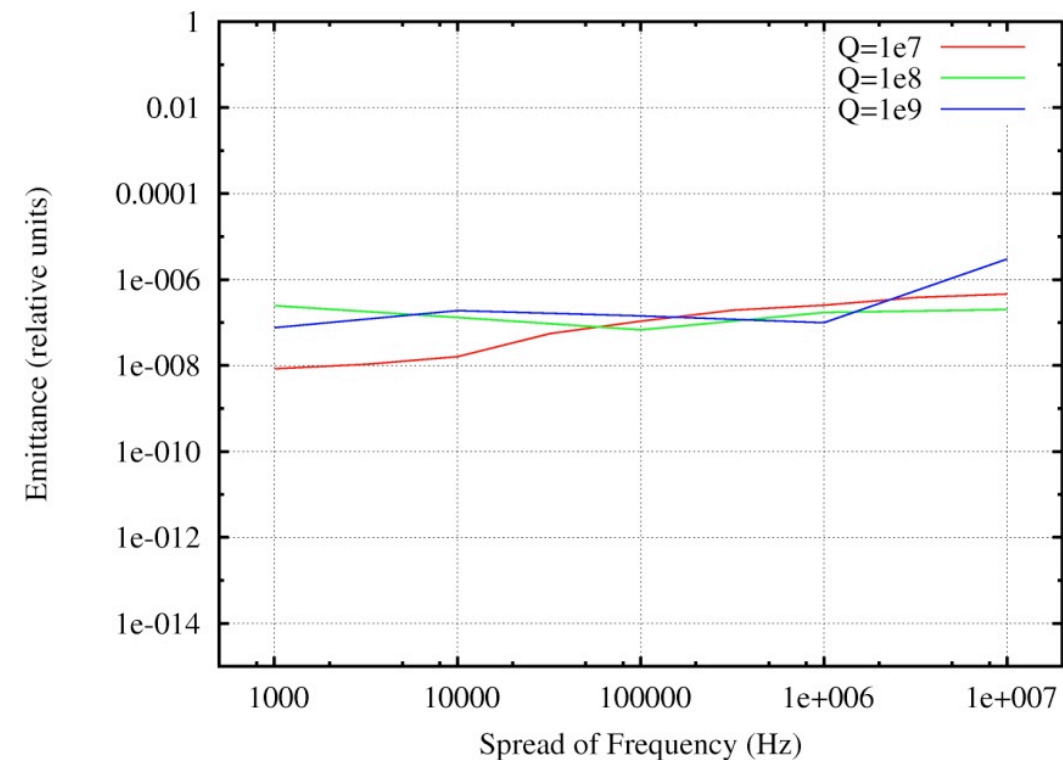
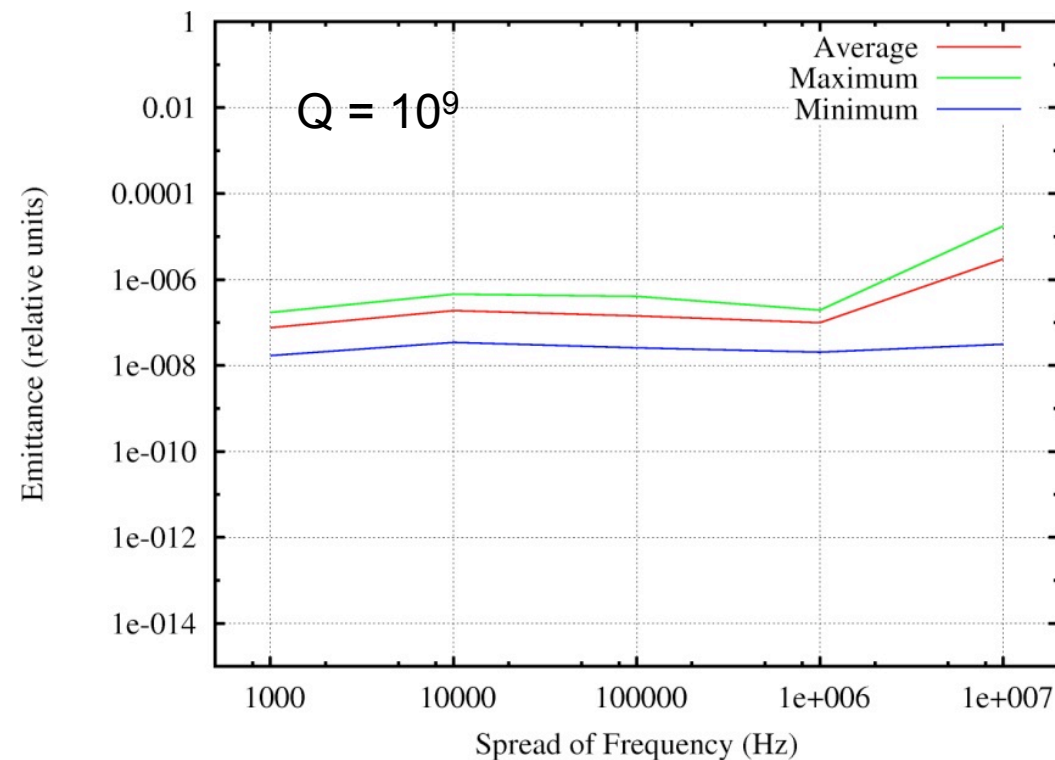
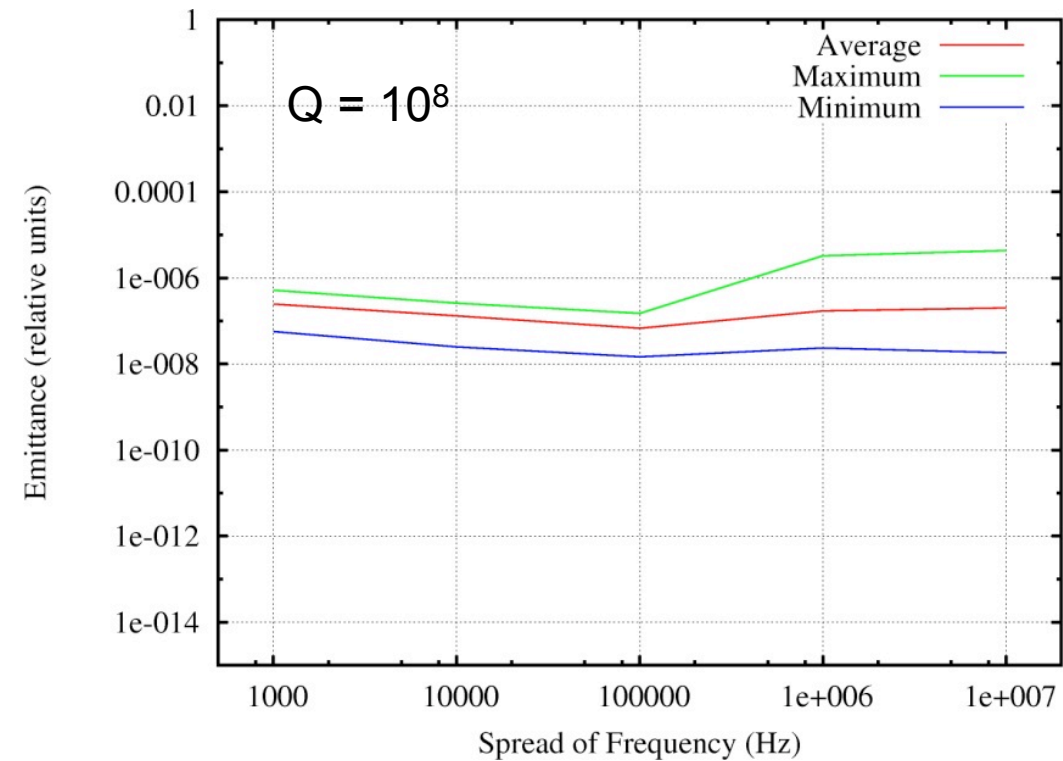
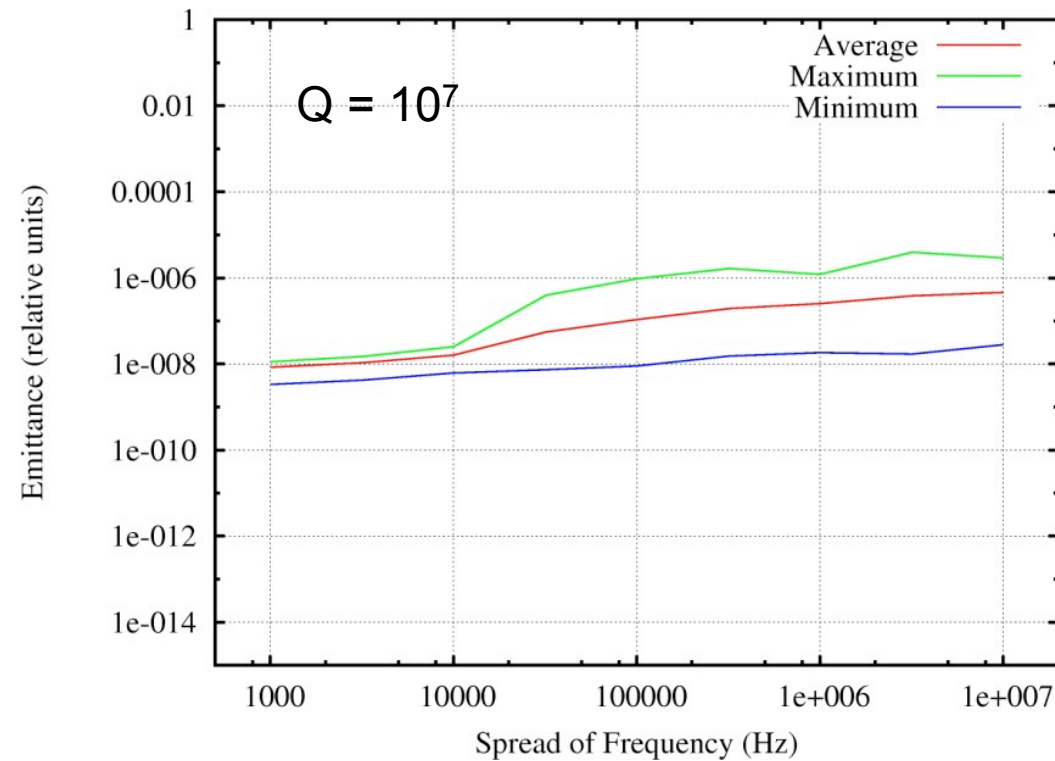
- “Realistic” linac: transverse emittance dilution vs δf (see TD-II-008)



- No noticeable effect

Collective Effects: Longitudinal Emittance

- “Klystron-type” instability: longitudinal emittance dilution vs δf



- No noticeable effect

Summary

- We studied mode of operation of Project X linac as a driver for Muon Collider with 15 Hz pulses of 6.7 ms with 50% DF and average current 5 mA (peak current 10 mA)
- We considered effects of incoherent losses, resonance excitation of monopole and dipole HOMs and collective effects in HE 650 MHz section of Project X linac
- We make a conclusion that these effects are small and we should be able to operate Project X linac as a driver for Muon Collider with specified beam parameters